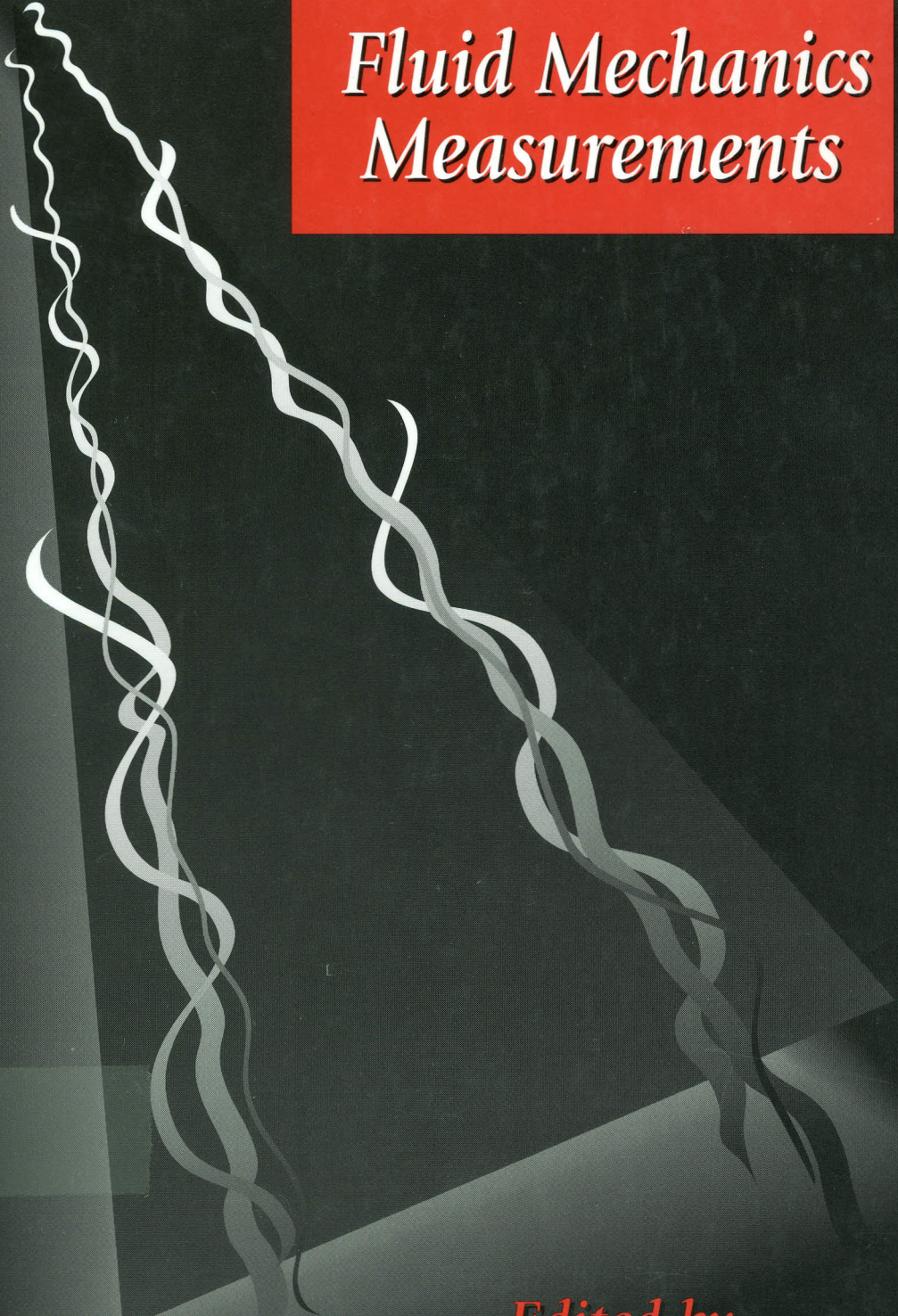


Second Edition

*Fluid Mechanics  
Measurements*



*Edited by  
Richard J. Goldstein*

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# FLUID MECHANICS MEASUREMENTS

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Second Edition

Edited by

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